Paper Reference(s)

6663/01 **Edexcel GCE**

Core Mathematics C1

Advanced Subsidiary

Monday 13 May 2013 – Afternoon

Time: 1 hour 30 minutes

Materials required for examination Mathematical Formulae (Pink)

Items included with question papers

Calculators may NOT be used in this examination.

Instructions to Candidates

Write the name of the examining body (Edexcel), your centre number, candidate number, the unit title (Core Mathematics C1), the paper reference (6663), your surname, initials and signature.

Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for the parts of questions are shown in round brackets, e.g. (2).

There are 11 questions in this question paper. The total mark for this paper is 75.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.

You must show sufficient working to make your methods clear to the Examiner.

Answers without working may not gain full credit.

1. Simplify

$$\frac{7+\sqrt{5}}{\sqrt{5}-1},$$

giving your answer in the form $a + b\sqrt{5}$, where a and b are integers.

(4)

2. Find

$$\int \left(10x^4 - 4x - \frac{3}{\sqrt{x}}\right) dx,$$

giving each term in its simplest form.

(4)

3. (a) Find the value of $8^{\frac{5}{3}}$.

(2)

(b) Simplify fully $\frac{(2x^{\frac{1}{2}})^3}{4x^2}$.

(3)

4. A sequence $a_1, a_2, a_3, ...$ is defined by

$$a_1 = 4$$
,

$$a_{n+1} = k(a_n + 2),$$
 for $n \ge 1$

where k is a constant.

(a) Find an expression for a_2 in terms of k.

(1)

Given that $\sum_{i=1}^{3} a_i = 2$,

(b) find the two possible values of k.

(6)

5. Find the set of values of x for which

(a)
$$2(3x+4) > 1-x$$
, (2)

(b)
$$3x^2 + 8x - 3 < 0$$
. (4)

6. The straight line L_1 passes through the points (-1, 3) and (11, 12).

(a) Find an equation for
$$L_1$$
 in the form $ax + by + c = 0$, where a , b and c are integers. (4)

The line L_2 has equation 3y + 4x - 30 = 0.

(b) Find the coordinates of the point of intersection of
$$L_1$$
 and L_2 . (3)

7. A company, which is making 200 mobile phones each week, plans to increase its production.

The number of mobile phones produced is to be increased by 20 each week from 200 in week 1 to 220 in week 2, to 240 in week 3 and so on, until it is producing 600 in week *N*.

(a) Find the value of
$$N$$
. (2)

The company then plans to continue to make 600 mobile phones each week.

(b) Find the total number of mobile phones that will be made in the first 52 weeks starting from and including week 1.

(5)

8.

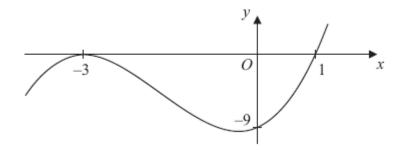


Figure 1

Figure 1 shows a sketch of the curve with equation y = f(x) where

$$f(x) = (x+3)^2(x-1), x \in \mathbb{R}.$$

The curve crosses the x-axis at (1, 0), touches it at (-3, 0) and crosses the y-axis at (0, -9).

(a) Sketch the curve C with equation y = f(x + 2) and state the coordinates of the points where the curve C meets the x-axis.

(3)

(b) Write down an equation of the curve C.

(1)

(c) Use your answer to part (b) to find the coordinates of the point where the curve C meets the y-axis.

(2)

9.

$$f'(x) = \frac{(3-x^2)^2}{x^2}, \quad x \neq 0.$$

(a) Show that $f'(x) = 9x^{-2} + A + Bx^2$, where A and B are constants to be found.

(3)

(b) Find f''(x).

(2)

Given that the point (-3, 10) lies on the curve with equation y = f(x),

(c) find f(x).

(5)

10. Given the simultaneous equations

$$2x + y = 1$$
$$x^2 - 4ky + 5k = 0$$

where k is a non zero constant,

(a) show that
$$x^2 + 8kx + k = 0$$
.

(2)

Given that $x^2 + 8kx + k = 0$ has equal roots,

(b) find the value of k.

(3)

(c) For this value of k, find the solution of the simultaneous equations.

(3)

11.

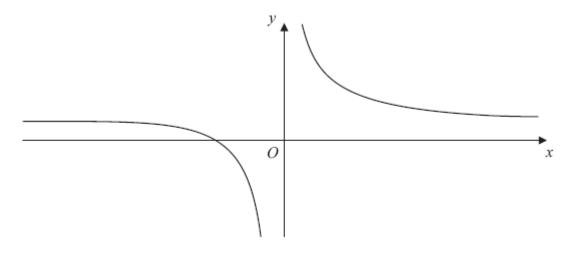


Figure 2

Figure 2 shows a sketch of the curve *H* with equation $y = \frac{3}{x} + 4$, $x \ne 0$.

(a) Give the coordinates of the point where H crosses the x-axis.

(1)

(b) Give the equations of the asymptotes to H.

(2)

(c) Find an equation for the normal to H at the point P(-3, 3).

(5)

This normal crosses the x-axis at A and the y-axis at B.

(d) Find the length of the line segment AB. Give your answer as a surd.

(3)

TOTAL FOR PAPER: 75 MARKS

END

$\frac{7+\sqrt{5}}{\sqrt{5}-1} \times \frac{(\sqrt{5}+1)}{(\sqrt{5}+1)}$ (Allow to multiply top and be $= \frac{\dots}{4}$ Note that M0A1 is not possible. The 4 multiply top and be $(7+\sqrt{5})(\sqrt{5}+1) = 7\sqrt{5}+5+7+\sqrt{5}$ $3+2\sqrt{5}$ Correct answer with no work	Obtains a denominator of 4 or sight of $(\sqrt{5}-1)(\sqrt{5}+1) = 4$	M1 A1cso
$= \frac{\dots}{4}$ Note that M0A1 is not possible. The 4 mu $(7 + \sqrt{5})(\sqrt{5} + 1) = 7\sqrt{5} + 5 + 7 + \sqrt{5}$ $3 + 2\sqrt{5}$	Obtains a denominator of 4 or sight of $(\sqrt{5}-1)(\sqrt{5}+1)=4$ 1st come from a correct method. An attempt to multiply the numerator by $(\pm\sqrt{5}\pm1)$ and get 4 terms with at least 2 correct for their $(\pm\sqrt{5}\pm1)$. (May be implied) Answer as written or $a=3$	M1
$(7+\sqrt{5})(\sqrt{5}+1) = 7\sqrt{5}+5+7+\sqrt{5}$ $3+2\sqrt{5}$	sight of $(\sqrt{5}-1)(\sqrt{5}+1)=4$ Ist come from a correct method. An attempt to multiply the numerator by $(\pm\sqrt{5}\pm1)$ and get 4 terms with at least 2 correct for their $(\pm\sqrt{5}\pm1)$. (May be implied) Answer as written or $a=3$	M1
$(7+\sqrt{5})(\sqrt{5}+1) = 7\sqrt{5}+5+7+\sqrt{5}$ $3+2\sqrt{5}$	An attempt to multiply the numerator by $(\pm\sqrt{5}\pm1)$ and get 4 terms with at least 2 correct for their $(\pm\sqrt{5}\pm1)$. (May be implied) Answer as written or $a=3$	
$3+2\sqrt{5}$	numerator by $(\pm\sqrt{5}\pm1)$ and get 4 terms with at least 2 correct for their $(\pm\sqrt{5}\pm1)$. (May be implied) Answer as written or $a=3$	
·	Answer as written or $a = 3$	A 1
Correct answer with no work	,	A1cso
	ing scores full marks	Γ/Ι
$\frac{7 + \sqrt{5}}{\sqrt{5} - 1} \times \frac{(-\sqrt{5} - 1)}{(-\sqrt{5} - 1)}$	Multiplies top and bottom by a correct expression. This statement is sufficient.	M1
(Allow to multiply top and bottom by $k(-\sqrt{5}-1)$)		
=4	Obtains a denominator of -4	A1cso
$(7+\sqrt{5})(-\sqrt{5}-1) = -7\sqrt{5}-5-7-\sqrt{5}$	An attempt to multiply the numerator by $(\pm \sqrt{5} \pm 1)$ and get 4 terms with at least 2 correct for their $(\pm \sqrt{5} \pm 1)$.	M1
$3+2\sqrt{5}$	Answer as written or $a = 3$ and $b = 2$	A1cso
Correct answer with no work	ing scores full marks	
A140mg 44:	noong Egyptions:	[4]
$\frac{(7+\sqrt{5})}{\sqrt{5}-1} = a+b\sqrt{5} \Rightarrow 7+\sqrt{5} =$ Multiplies and collects rationa $a-b=1, 5b-a$ Correct equat $a=3, b=$	$(a-b)\sqrt{5} + 5b - a \text{ M1}$ al and irrational parts $= 7 \text{ A1}$ itions 2	
	(Allow to multiply top and bo $= \frac{\dots}{-4}$ $(7+\sqrt{5})(-\sqrt{5}-1) = -7\sqrt{5} - 5 - 7 - \sqrt{5}$ $3+2\sqrt{5}$ Correct answer with no work $\frac{(7+\sqrt{5})}{\sqrt{5}-1} = a+b\sqrt{5} \Rightarrow 7+\sqrt{5} = 0$ Multiplies and collects rations $a-b=1, 5b-a$ Correct equat $a=3, b=1$	$\frac{7+\sqrt{3}}{\sqrt{5}-1} \times \frac{(-\sqrt{3}-1)}{(-\sqrt{5}-1)}$ correct expression. This statement is sufficient. (Allow to multiply top and bottom by $k(-\sqrt{5}-1)$) $= \frac{\dots}{-4}$ Obtains a denominator of -4 An attempt to multiply the numerator by $(\pm\sqrt{5}\pm1)$ and get 4 terms with at least 2 correct for their $(\pm\sqrt{5}\pm1)$. (May be implied) $3+2\sqrt{5}$ Answer as written or $a=3$

Question Number	Schen	ne	Marks
2	$(\int =)\frac{10x^5}{5} - \frac{4x^2}{2}, -\frac{3x^{\frac{1}{2}}}{\frac{1}{2}}$	M1: Some attempt to integrate: $x^n \to x^{n+1}$ on at least one term. (not for + c) (If they think $\frac{3}{\sqrt{x}}$ is $3x^{\frac{1}{2}}$ you can still award the method mark for $\frac{\frac{1}{x^2} \to x^{\frac{3}{2}}}{5}$ A1: $\frac{10x^5}{5}$ and $\frac{-4x^2}{2}$ or better A1: $-\frac{3x^{\frac{1}{2}}}{\frac{1}{2}}$ or better	M1A1, A1
	$= \underline{2x^5 - 2x^2 - 6x^{\frac{1}{2}} + c}$ Do not apply isw. If they obtain the corrective lose the l		A1
	1111	Annual Control of Cont	[4]

Question Number	Scho	eme	Marks
3(a)	$8^{\frac{1}{3}} = 2$ or $8^5 = 32768$	A correct attempt to deal with the $\frac{1}{3}$ or the 5. $8^{\frac{1}{3}} = \sqrt[3]{8}$ or $8^5 = 8 \times 8 \times 8 \times 8 \times 8$	M1
	$\left(8^{\frac{5}{3}} = \right) 32$	Cao	A1
	A correct answer with no		
	Alterr		
	$8^{\frac{5}{3}} = 8 \times 8^{\frac{2}{3}} = 8 \times 2^2 = N$ = 32		
			(2)
(b)	$\left(2x^{\frac{1}{2}}\right)^3 = 2^3 x^{\frac{3}{2}}$	One correct power either 2^3 or $x^{\frac{3}{2}}$. $ \left(2x^{\frac{1}{2}}\right) \times \left(2x^{\frac{1}{2}}\right) \times \left(2x^{\frac{1}{2}}\right) $ on its own is not sufficient for this mark.	M1
	$\frac{8x^{\frac{3}{2}}}{4x^2} = 2x^{-\frac{1}{2}} \text{ or } \frac{2}{\sqrt{x}}$	M1: Divides coefficients of x and subtracts their powers of x. Dependent on the previous M1	dM1A1
		A1: Correct answer	
	Note that unless the power of <i>x</i> imp	blies that they have subtracted their	
	powers you would need to see evide	$\exists \lambda$	
	would score dM0 unless you see some evidence that $3/2 - 2$ was intended for the power of x .		
	Note that there is a misconception that	$\left(2x^{\frac{1}{2}}\right)^3$ $\left(\frac{1}{2x^2}\right)^3$	
			(3)
			[5]

Question Number	Scheme		Marks	
	For this question, mark (a) and (b) together and ignore labelling.		
4(a)	$(a_2 =) k(4+2) (= 6k)$	Any correct (possibly un-simplified) expression	B1	
			(1)	
(b)	$a_3 = k$ (their $a_2 + 2$) (= $6k^2 + 2k$)	An attempt at a_3 . Can follow through their answer to (a) but a_2 must be an expression in k .	M1	
	$a_1 + a_2 + a_3 = 4 + (6k) + (6k^2 + 2k)$	An attempt to find their $a_1 + a_2 + a_3$	M1	
	$4 + (6k) + (6k^2 + 2k) = 2$	A correct equation in any form.	A1	
	Solves $6k^2 + 8k + 2 = 0$ to obtain $k = (6k^2 + 8k + 2 = 2(3k + 1)(k + 1))$	Solves their 3TQ as far as $k =$ according to the general principles. (An independent mark for solving their three term quadratic)	M1	
	k = -1/3	Any equivalent fraction	A1	
	<i>k</i> = −1	Must be from a correct equation. (Do not accept un-simplified)	B1	
	Note that it is quite common to think that, this is likely only to score the M1	ne sequence is an AP. Unless they find		
			(6)	
			[7]	

Question Number	S	cheme	Marks	;
5 (a)	6x + x > 1 - 8	Attempts to expand the bracket and collect x terms on one side and constant terms on the other. Condone sign errors and allow one error in expanding the bracket. Allow $<$, \leq , \geq ,= instead of $>$.	M1	
	x > -1	Cao	A1	
	Do not isw here, r	nark their final answer.		
				(2)
(b)	(x+3)(3x-1)[=0]	M1: Attempt to solve the quadratic to obtain two critical values		
	$\Rightarrow x = -3 \text{ and } \frac{1}{3}$	A1: $x = -3$ and $\frac{1}{3}$ (may be implied by their inequality). Allow all equivalent	M1A1	
		fractions for -3 and 1/3. (Allow 0.333 for 1/3)		
		M1: Chooses "inside" region (The letter <i>x</i> does not need to be used here)		
	1	A1ft: Allow $x < \frac{1}{3}$ and $x > -3$ or $\left(-3, \frac{1}{3}\right)$ or $x < \frac{1}{3} \cap x > -3$. Follow		
	$-3 < x < \frac{1}{3}$	through their critical values. (must be in terms of x here) Allow all equivalent fractions for -3 and 1/3.	M1A1ft	
		Both $(x < \frac{1}{3}$ or $x > -3)$ and $(x < \frac{1}{3}, x > -3)$ as a final answer		
		score A0.		
				(4)
				[6]
		an otherwise correct answer in (a) or (b) l once, the first time it occurs.		

Question Number	Schen	me	Marks	
6	(-1, 3) ,	(11, 12)		
(a)	$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{12 - 3}{11 - (-1)}, = \frac{3}{4}$	M1:Correct method for the gradient A1: Any correct fraction or decimal	M1,A1	
	$y-3 = \frac{3}{4}(x+1)$ or $y-12 = \frac{3}{4}(x-11)$ or $y = \frac{3}{4}x + c$ with attempt at substitution to find c	Correct straight line method using either of the given points and a numerical gradient.	M1	
	4y - 3x - 15 = 0	Or equivalent with integer coefficients (= 0 is required)	A1	
	This A1 should only	be awarded in (a)		
			(4)	
(a) Way 2	$\frac{y - y_1}{y_2 - y_1} = \frac{x - x_1}{x_2 - x_1} \Rightarrow \frac{y - 3}{12 - 3} = \frac{x + 1}{11 + 1}$	M1: Use of a correct formula for the straight line	M1A1	
way 2	$y_2 - y_1$ $x_2 - x_1$ $12 - 3$ $11 + 1$	A1: Correct equation		
	12(y-3) = 9(x+1)	Eliminates fractions	M1	
	4y - 3x - 15 = 0	Or equivalent with integer coefficients (= 0 is required)	A1	
			(4)	
(b)	Solves their equation from part (a) and L_2 simultaneously to eliminate one variable	Must reach as far as an equation in <i>x</i> only or in <i>y</i> only. (Allow slips in the algebra)	M1	
	x = 3 or y = 6	One of $x = 3$ or $y = 6$	A1	
	Both $x = 3$ and $y = 6$	Values can be un-simplified fractions.	A1	
	Fully correct answers with no	working can score 3/3 in (b)		
			(3)	
71.	(12)			
(b) Way 2	$(-1,3) \rightarrow -a + 3b + c = 0$ $(11,12) \rightarrow 11a + 12b + c = 0$	Substitutes the coordinates to obtain two equations	M1	
	$\therefore a = -\frac{3}{4}b, \ b = -\frac{4}{15}c$ e.g. $c = 1 \Rightarrow b = -\frac{4}{15}, \ a = \frac{3}{15}$	Obtains sufficient equations to establish values for <i>a</i> , <i>b</i> and <i>c</i>	A1	
	e.g. $c = 1 \Rightarrow b = -\frac{4}{15}$, $a = \frac{3}{15}$	Obtains values for a, b and c	M1	
	$\frac{3}{15}x - \frac{4}{15}y + 1 = 0 \Rightarrow 4y - 3x - 15 = 0$	Correct equation	A1	
			(4)	
			[7]	

Question Number	Scheme		
7(a)	$600 = 200 + (N-1)20 \Rightarrow N = \dots$	Use of 600 with a correct formula in an attempt to find <i>N</i> . A correct formula could be implied by a correct answer.	M1
	<i>N</i> = 21	cso	A1
	Accept correct an	swer only.	
	20	1 (correct formula implied)	
	Listing: All terms must be listed up to		
	A solution that scores 2 if fully	correct and 0 otherwise.	
(1.)	T . 1 6 A	D.6°4.	(2)
(b)	Look for an A $S = \frac{21}{2}(2 \times 200 + 20 \times 20) \text{ or } \frac{21}{2}(200 + 600)$ or $S = \frac{20}{2}(2 \times 200 + 19 \times 20) \text{ or } \frac{20}{2}(200 + 580)$ $(= 8400 \text{ or } 7800)$ Then for the cons	M1: Use of correct sum formula with their integer $n = N$ or $N - 1$ from part (a) where $3 < N < 52$ and $a = 200$ and $d = 20$. A1: Any correct un-simplified numerical expression with $n = 20$ or $n = 21$ (No follow through here)	M1A1 M1A1ft
	So total is 27000	Cao	A1
	Note that for the constant terms, they may o	correctly use an AP sum with $d = 0$.	
	There are no marks in (b)	<u> </u>	
	. (.)	, va	(5)
			[7]
	If they obtain $N = 20$ in (a) $(0/2)$ ar $S = \frac{20}{2}(2 \times 200 + 19 \times 20) + 32 \times 600$ allow them to 'recover' and so Similarl If they obtain $N = 22$ in (a) $(0/2)$ ar $S = \frac{21}{2}(2 \times 200 + 20 \times 20) + 31 \times 600$ allow them to 'recover' and so	$0 = 7800 + 19\ 200 = 27\ 000$ score full marks in (b) y and then in (b) proceed with, $0 = 8400 + 18\ 600 = 27\ 000$	

Question Number	Schem	ne	Marks
8	<i>/</i> -	Horizontal translation – does not have to cross the <i>y</i> -axis on the right but must at least reach the <i>x</i> -axis.	B1
(a)	-6 -2 -10 -	Touching at (-5, 0). This could be stated anywhere or -5 could be marked on the <i>x</i> -axis. Or (0, -5) marked in the correct place. Be fairly generous with 'touching' if the intention is clear.	B1
	7 -10	The right hand tail of their cubic shape crossing at (-1, 0). This could be stated anywhere or -1 could be marked on the <i>x</i> -axis. Or (0, -1) marked in the correct place. The curve must cross the <i>x</i> -axis and not stop at -1.	B1
		•	(3)
(b)	$(x+5)^2(x+1)$	Allow $(x+3+2)^2(x-1+2)$	B1
			(1)
(c)	When $x = 0$, $y = 25$	M1: Substitutes $x = 0$ into their expression in part (b) which is not $f(x)$. This may be implied by their answer. Note that the question asks them to use part (b) but allow independent methods. A1: $y = 25$ (Coordinates not needed)	M1 A1
	If they expand <u>incorrectly</u> prior to s	,	
	NB $f(x + 2) = x^3 + 1$		
			(2)
			[6]

Question Number	Scheme		
9 (a)	$(3-x^2)^2 = 9 - 6x^2 + x^4$	An attempt to expand the numerator obtaining an expression of the form $9 \pm px^2 \pm qx^4$, $p, q \neq 0$	M1
	$9x^{-2} + x^2$	Must come from $\frac{9+x^4}{x^2}$	A1
	-6	Must come from $\frac{-6x^2}{x^2}$	A1
	Alternative 1: Writes $\frac{(3-x^2)^2}{x^2}$ as	s $(3x^{-1} - x)^2$ and attempts to expand = M1	
	then A1A	1 as in the scheme.	
		$Ax^2 + Bx^4$, expands $(3-x^2)^2$ and compares hen A1A1 as in the scheme.	
			(3)
	(f'(x))	$=9x^{-2}-6+x^2$	
(b)	$-18x^{-3} + 2x$	M1: $x^n \to x^{n-1}$ on separate terms at least once. Do not award for $A \to 0$ (Integrating is M0) A1ft: $-18x^{-3} + 2"B"x$ with a numerical B and no extra terms. (A may have been incorrect or even zero)	M1 A1ft
		incorrect of even zero)	(2)
(c)	$f(x) = -9x^{-1} - 6x + \frac{x^3}{3}(+c)$	M1: $x^n \to x^{n+1}$ on separate terms at least once. (Differentiating is M0) A1ft: $-9x^{-1} + Ax + \frac{Bx^3}{3}(+c)$ with	M1A1ft
	2	numerical A and B, $A, B \neq 0$	
	$10 = \frac{-9}{-3} - 6(-3) + \frac{(-3)^3}{3} + c \text{ so } c$ $= \dots$	Uses $x = -3$ and $y = 10$ in what they think is $f(x)$ (They may have differentiated here) but it must be a changed function i.e. not the original $f'(x)$, to form a linear equation in c and attempts to find c . No $+ c$ gets M0 and A0 unless their method implies that they are correctly finding a constant.	M1
	c = -2	cso	A1
	$(f(x) =) -9x^{-1} - 6x + \frac{x^3}{3} + \text{their}$	Follow through their c in an otherwise (possibly un-simplified) correct expression . Allow $-\frac{9}{x}$ for $-9x^{-1}$ or even $\frac{9x^{-1}}{-1}$.	A1ft
		no marks there but if they then go on to	
	use their integration in (c), th	e marks for integration are available.	
			(5)
			[10]

Question Number	Scheme	Marks		
10(a)	$x^2 - 4k(1 - 2x) + 5k(=0)$	Makes y the subject from the first equation and substitutes into the second equation (= 0 not needed here) or eliminates y by a correct method.	M1	
	So $x^2 + 8kx + k = 0 *$	Correct completion to printed answer. There must be no incorrect statements.	A1cso	
(b)	$(8k)^2 - 4k$	M1: <u>Use</u> of $b^2 - 4ac$ (Could be in the quadratic formula or an inequality, = 0 not needed yet). There must be some correct substitution but there must be no x 's. No formula quoted followed by e.g. $8k^2 - 4k = 0$ is M0. A1: Correct expression. Do not condone missing brackets unless they are implied by later work but can be implied by $(8k)^2 > 4k$ etc.	M1 A1	(2)
	$k = \frac{1}{16} \text{ (oe)}$	Cso (Ignore any reference to $k = 0$) but there must be no contradictory earlier statements. A fully correct solution with no errors.	A1	(3)
(b)	$\Rightarrow x^2 + 8kx + k = (x + \sqrt{k})^2$	M1: Correct strategy for equal roots		(3)
Way 2 Equal roots	$\Rightarrow 8k = 2\sqrt{k}$	A1: Correct equation	M1A1	
	$k = \frac{1}{16} \text{ (oe)}$	Cso (Ignore any reference to $k = 0$)	A1	
(1)	Completes the Square $x^2 + 8kx + k = (x + 4k)^2 - 16k^2 + k$	M1: $(x \pm 4k)^2 \pm p \pm k$, $p \neq 0$		
(b) Way 3	$\Rightarrow 16k^2 - k = 0$	A1: Correct equation	M1A1	
	$k = \frac{1}{16} \text{ (oe)}$	Cso (Ignore any reference to $k = 0$)	A1	
(c)	$x^{2} + \frac{1}{2}x + \frac{1}{16} = 0$ so $(x + \frac{1}{4})^{2} = 0 \Rightarrow x =$	Substitutes their value of k into the given quadratic and attempt to solve their 2 or 3 term quadratic as far as $x = $ (may be implied by substitution into the quadratic formula) or starts again and substitutes their value of k into the second equation and solves simultaneously to obtain a value for x .	M1	(3)
	$x = -\frac{1}{4}, y = 1\frac{1}{2}$	First A1 one answer correct, second A1 both answers correct.	A1A1	
	Special Case: $x^2 + \frac{1}{2}x + \frac{1}{16} = 0 \implies$	$x = -\frac{1}{4}, \frac{1}{4} \Rightarrow y = 1\frac{1}{2}, \frac{1}{2} \text{ allow M1A1A0}$		
				(3) [8]

Question Number	Sche	eme	Marks
11 (a)	$\left(-\frac{3}{4}, 0\right)$. Accept $x = -\frac{3}{4}$		B1
			(1)
(b)	y = 4	B1: One correct asymptote	
	x = 0 or 'y-axis'	B1: Both correct asymptotes and no extra ones.	B1B1
	Special case $x \neq 0$ and	d $y \neq 4$ scores B1B0	
	-		(2)
(c)	$\frac{\mathrm{d}y}{\mathrm{d}x} = -3x^{-2}$	$\frac{dy}{dx} = kx^{-2} \text{ (Allow } \frac{dy}{dx} = kx^{-2} + 4\text{)}$	M1
	At $x = -3$, gradient of curve $= -\frac{1}{3}$	Cao (may be un-simplified but must be a fraction with no powers) e.g. $-3(-3)^{-2}$ scores A0 unless evaluated as e.g. $\frac{-3}{9}$ or is implied by their normal gradient.	A1
	Gradient of normal = $-1/m$	Correct perpendicular gradient rule applied to a numerical gradient that must have come from substituting <i>x</i> = -3 into their derivative. Dependent on the previous M1.	dM1
	Normal at <i>P</i> is $(y-3) = 3(x+3)$	M1: Correct straight line method using (-3, 3) and a "changed" gradient. A wrong equation with no formula quoted is M0. Also dependent on the first M1. A1: Any correct equation	dM1A1
			(5)
(d)	(-4, 0) and (0, 12).	Both correct	B1
	So AB has length $\sqrt{160}$ or AB^2 has length 160	(May be seen on a sketch) M1: Correct use of Pythagoras for their <i>A</i> and <i>B</i> one of which lies on the <i>x</i> -axis and the other on the <i>y</i> -axis, obtained from their equation in (c). A correct method for AB^2 or AB . A1: $\sqrt{160}$ or better e.g. $4\sqrt{10}$ with no errors seen	M1 A1cso
			(3)
			[11]